

3. The triangle PQR is such that $\vec{PQ} = 3\mathbf{i} + 5\mathbf{j}$ and $\vec{PR} = 13\mathbf{i} - 15\mathbf{j}$

(a) Find \vec{QR}

(2)

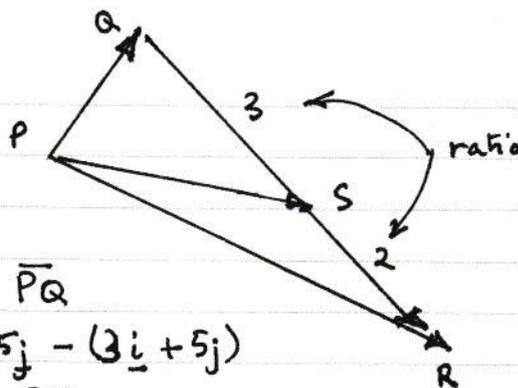
(b) Hence find $|\vec{QR}|$ giving your answer as a simplified surd.

(2)

The point S lies on the line segment QR so that $QS:SR = 3:2$

(c) Find \vec{PS}

(2)



$$\begin{aligned} \text{(a)} \quad \vec{PQ} + \vec{QR} &= \vec{PR} \\ \vec{QR} &= \vec{PR} - \vec{PQ} \\ &= 13\mathbf{j} - 15\mathbf{j} - (3\mathbf{i} + 5\mathbf{j}) \\ &= 10\mathbf{j} - 20\mathbf{j} \end{aligned}$$

$$\text{(b)} \quad |\vec{QR}| = \sqrt{10^2 + 20^2} = \sqrt{500} = \underline{10\sqrt{5}}$$

Draw in S and \vec{PS}

$$\begin{aligned} \text{(c)} \quad \vec{PS} &= \vec{PQ} + \frac{3}{5}\vec{QR} \\ &= 3\mathbf{j} + 5\mathbf{j} + \frac{3}{5}(10\mathbf{i} - 20\mathbf{j}) \\ &= 3\mathbf{i} + 5\mathbf{j} + 6\mathbf{i} - 12\mathbf{j} \\ &= \underline{9\mathbf{i} - 7\mathbf{j}} \end{aligned}$$

