

14. (i) A student states

"if  $x^2$  is greater than 9 then  $x$  must be greater than 3"

Determine whether or not this statement is true, giving a reason for your answer.

(1)

- (ii) Prove that for all positive integers  $n$ ,

$$n^3 + 3n^2 + 2n$$

is divisible by 6

(3)

(i) If  $x$  is -ve eg -5 then  $x^2 = 25$  so  $x^2 > 9$   
 But  $x$  is -5 which is less than 3.  
So the statement is false.

(ii) Factorise  $n^3 + 3n^2 + 2n$   
 $n(n^2 + 3n + 2)$   
 $n(n+1)(n+2)$ .

So the given expression is the product of  
3 consecutive numbers.

So of these 3 numbers one is bound to be a  
 multiple of 2 and another is bound to be a multiple  
 of 3.

So the numbers multiplied together must be  
a multiple of 6.

